





It's important to realize exactly what we're modeling.

The idea behind hidden Markov models is <u>not</u> that the sequence is random, but that the sequence we observe is <u>one of many possible</u> <u>instances</u> of some underlying process or object.

E.g., actin differs slightly from organism to organism.

Imagine an "ideal", but unobservable, actin, defined by specific underlying physicochemical properties important for its function. What we see in nature is not this ideal gene, but many variants, all just a bit different.

In the hidden Markov model, the underlying process or structure is represented as hidden, unobservable *states* and the observed sequences represent <u>possible</u> sequences compatible with these states.

We say that the observed sequence is *emitted* from the hidden states.





Now, imagine a sequence of coin flips generated by these 2 coins, one fair and one biased.

To decide if a sequence of coin flips comes from the biased or fair coin, we could evaluate the **ratio of the probabilities** of observing the sequence by each model:

P(X | fair coin)

P(X | biased coin)

Does this remind you of something we've seen before? How might we test where the fair & biased coins were swapped along a long stretch of coin flips?

Answer: Yes. Use the *forward algorithm*. We'll see this shortly.

Important questions we might like to ask:

5. How do we choose the best HMM topology from the many possible choices?

Answer: Good question. No great answer.

Often trial-and-error, and understanding the essential features of the system that you are modeling.

Each of these algorithms (the Viterbi, forward, and forward-backward) uses dynamic programming to find an optimal solution.

(just like aligning sequences)

Given a DNA sequence X (e.g., CGATCGCG), how do we find the most probable sequence of states (e.g., ----++++)?

→ The Viterbi algorithm

We want to find the state path that maximizes the probability of observing that sequence from that HMM model.

Viterbi does this recursively using dynamic programming.

As with sequence alignment, we'll construct a path matrix that captures the best score (*i.e.*, highest probability) along a single path through the HMM up to each position. We'll "grow" this matrix using a few simple recursion rule.

How do we calculate the probability of a sequence given our HMM model?

\rightarrow The forward algorithm

Subtle difference from Viterbi: Viterbi gives the probability of the sequence being derived from the model *given the optimal state path.*

The forward algorithm takes into account all possible state paths.

Again, it does this recursively using dynamic programming.

