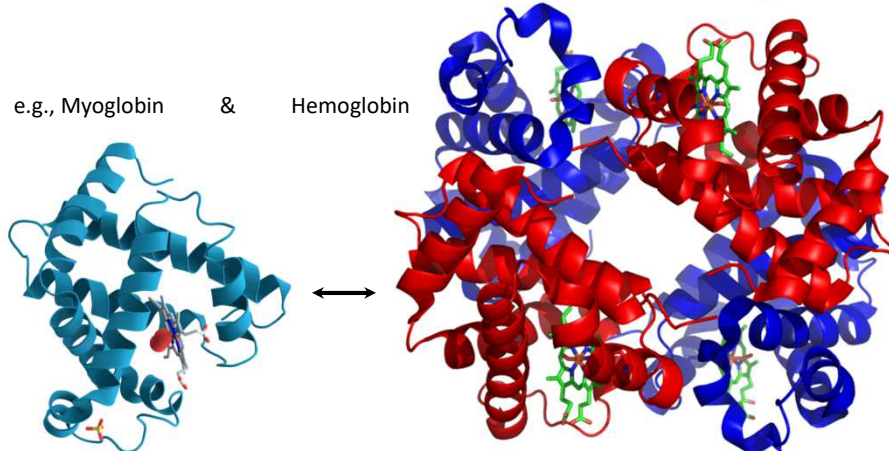


Typically, to be “biologically related” means to share a common ancestor. In biology, we call this *homologous*.

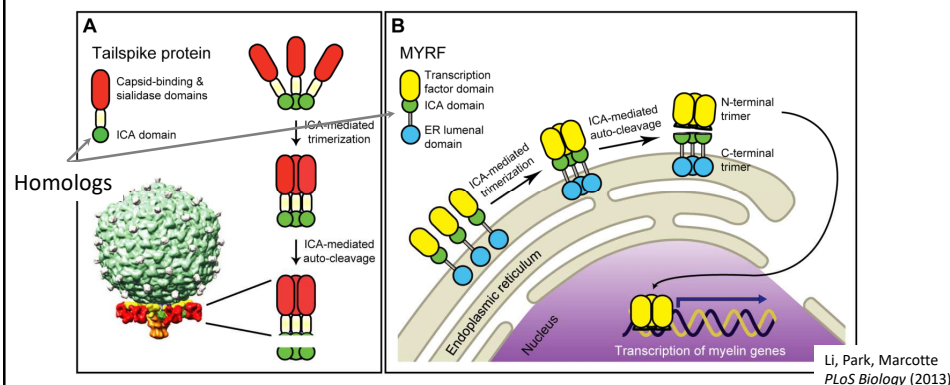
Two proteins sharing a common ancestor are said to be *homologs*. Homology often implies structural similarity & sometimes (not always) sequence similarity. A statistically significant sequence or structural similarity can be used to infer homology (common ancestry).



1

In practice, searching for sequence or structural similarity is one of the most powerful computational approaches to discover a gene’s function. We can often gain insight about a protein from its homologs.

For example, my lab discovered that myelinating the neurons in your brain reuses the same biochemical mechanism that phage use to make capsids. The key breakthrough was recognizing that the human and phage proteins contained homologous domains.

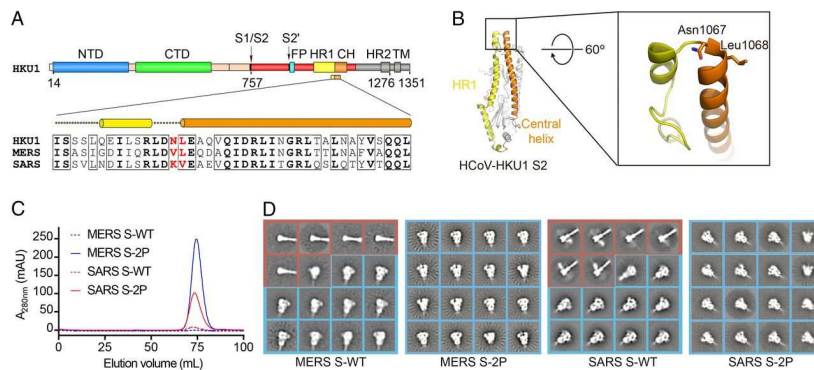


2

& for a very timely example, here's the "trillion dollar" paper from the McLellan lab that the SARS-CoV-2 vaccines are designed from based on homology to MERS and SARS spike antigens

Immunogenicity and structures of a rationally designed prefusion MERS-CoV spike antigen

Jesper Pallesen, Nianshuang Wang, Kizmekia S. Corbett, Daniel Wrapp, Robert N. Kirchdoerfer, Hannah L. Turner, Christopher A. Cobelli, Michelle M. Becker, Lingfeng Wang, Wei Shi, Wing-Pui Kong, Erica L. Andres, Aminja N. Kettenbach, Mark R. Denison, James D. Chappell, Barney S. Graham, Andrew B. Ward, and Jason S. McLellan
 PNAS August 29, 2017 114 (35): E7348–E7357; first published August 14, 2017; https://doi.org/10.1073/pnas.1707284114



3

Sequence alignment algorithms such as BLAST, PSI-BLAST, FASTA, and the Needleman–Wunsch & Smith-Waterman algorithms arguably comprise some of the most important driver technologies of modern biology and underlie the sequencing revolution.

So, let's start learning bioinformatics algorithms by learning how to align two protein sequences.

4

Live demo:

http://blast.ncbi.nlm.nih.gov/Blast.cgi?PROGRAM=blastp&BLAST_PROGRAMS=blastp&PAGE_TYPE=BlastSearch&SHOW_DEFAULTS=on&LINK_LOC=blasthome

MVLSPADKTNVKAAWGKVGAGHAGEYGAEALERMFLSFPTTKTYFPHFDLSHGSAQVKGHG
KKVADALTNAVAHVDDMPNALSALSDLHAHKLRVDPVNFKLLSHCLLVTLAAHLPAEFTP
AVHASLDKFLASVSTVLTSKYR

The next few slides show the data from searching this dbase, so #'s are bit different from the live version:

Title: All non-redundant GenBank CDS translations+PDB+SwissProt+PIR+PRF excluding environmental samples from WGS projects

Molecule Type: Protein

Update date: 2021/01/12

Number of sequences: 340,795,435

5

Descriptions

Graphic Summary

Alignments

Taxonomy

Sequences producing significant alignments

Download

New Select columns

Show

100

?

select all

100 sequences selected

GenPept

Graphics

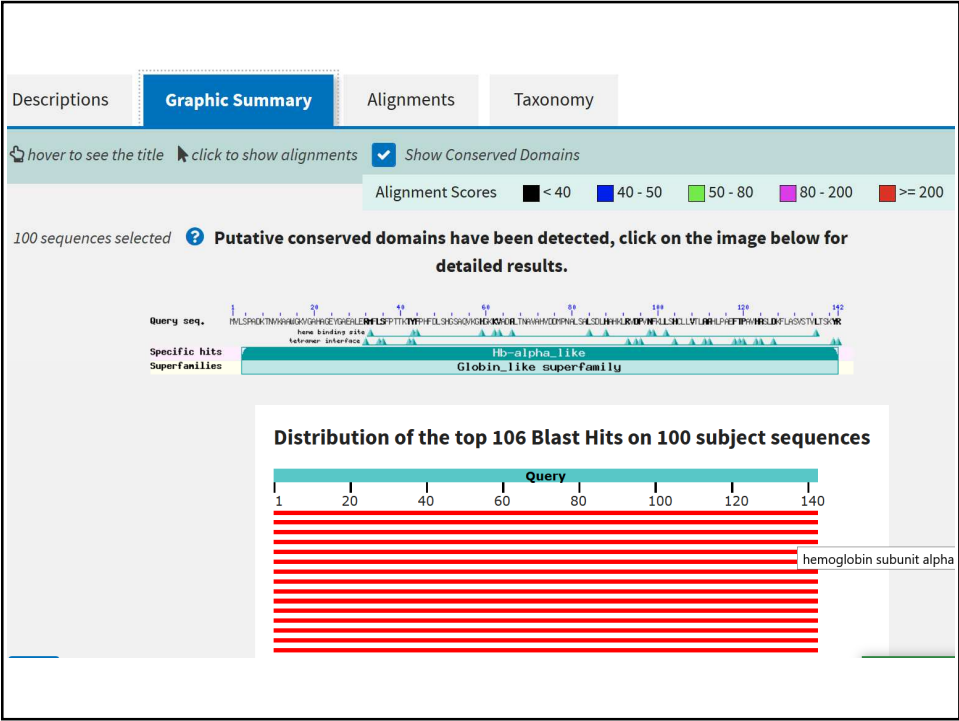
Distance tree of results

Multiple alignment

New MSA Viewer

	Description	Scientific Name	Max Score	Total Score	Query Cover	E value	Per. Ident	Acc. Len	Accession
<input checked="" type="checkbox"/>	hemoglobin alpha 2 [synthetic construct]	synthetic construct	287	287	100%	9e-98	100.00%	143	AAV29522.1
<input checked="" type="checkbox"/>	hemoglobin alpha subunit family protein [Citrobacter freundii]	Citrobacter freundii	286	286	100%	1e-97	100.00%	142	VYP_108961785.1
<input checked="" type="checkbox"/>	A cis-proline in alpha-hemoglobin stabilizing Protein directs the structural reorganization of alpha-hemoglobin [Homo sapiens]	Homo sapiens	286	286	100%	2e-97	100.00%	145	3IA3_B
<input checked="" type="checkbox"/>	mutant hemoglobin alpha 2 globin chain [Homo sapiens]	Homo sapiens	286	286	100%	2e-97	99.30%	142	AK266543.1
<input checked="" type="checkbox"/>	mutant hemoglobin subunit alpha 2 [Homo sapiens]	Homo sapiens	286	286	100%	3e-97	99.30%	142	AYY55002.1
<input checked="" type="checkbox"/>	hemoglobin alpha-2 [Homo sapiens]	Homo sapiens	285	285	100%	4e-97	99.30%	142	AAH04486.1
<input checked="" type="checkbox"/>	alpha-2-globin [Homo sapiens]	Homo sapiens	285	285	100%	5e-97	99.30%	142	AAF72612.1
<input checked="" type="checkbox"/>	TPA-globin C1 [Homo sapiens]	Homo sapiens	286	286	100%	6e-97	100.00%	177	SAIB2135.1
<input checked="" type="checkbox"/>	hemoglobin subunit alpha [Gorilla gorilla gorilla]	Gorilla gorilla gorilla	285	285	100%	7e-97	99.30%	142	XP_030858702.1
<input checked="" type="checkbox"/>	hemoglobin alpha 1-2 hybrid [Homo sapiens]	Homo sapiens	284	284	100%	1e-96	99.30%	142	ABF56145.1
<input checked="" type="checkbox"/>	mutant hemoglobin subunit alpha 2 [Homo sapiens]	Homo sapiens	284	284	100%	1e-96	99.30%	142	AYY54998.1
<input checked="" type="checkbox"/>	mutant hemoglobin subunit alpha 2 [Homo sapiens]	Homo sapiens	284	284	100%	1e-96	99.30%	142	AYY55003.1
<input checked="" type="checkbox"/>	mutant hemoglobin subunit alpha 2 [Homo sapiens]	Homo sapiens	284	284	100%	1e-96	99.30%	142	AYY55001.1
<input checked="" type="checkbox"/>	Hemoglobin Thionville, An Alpha-Chain Variant With A Substitution Of A Glutamate For Valine At Na-1 And Havi	Homo sapiens	284	284	100%	1e-96	99.30%	143	1BAG_A
<input checked="" type="checkbox"/>	hemoglobin alpha-1 globin chain [Homo sapiens]	Homo sapiens	284	284	100%	1e-96	99.30%	142	AAK37554.1
<input checked="" type="checkbox"/>	Hemoglobin (Val Beta1 Met Trp Beta37 Tyr) Mutant [Homo sapiens]	Homo sapiens	284	284	99%	2e-96	100.00%	141	1A00_A
<input checked="" type="checkbox"/>	alpha 2 globin variant [Homo sapiens]	Homo sapiens	284	284	100%	2e-96	99.30%	142	BAD97112.1

6



7

Descriptions **Graphic Summary** **Alignments** Taxonomy

Alignment view Pairwise Download

100 sequences selected

[Download](#) [GenPept](#) [Graphics](#) Next Previous Descriptions

hemoglobin alpha 2, partial [synthetic construct]
Sequence ID: [AAX29522.1](#) Length: 143 Number of Matches: 1

Range 1: 1 to 142 [GenPept](#) [Graphics](#) Next Match Previous Match

Score	Expect	Method	Identities	Positives	Gaps
287 bits(734)	7e-98	Compositional matrix adjust.	142/142(100%)	142/142(100%)	0/142(0%)
Query 1	MVLSPADKTNVKAAGKVGAGHAGEYGAELERMFLSFPTTKTYFPHFDLSHGSA				
Sbjct 1	MVLSPADKTNVKAAGKVGAGHAGEYGAELERMFLSFPTTKTYFPHFDLSHGSA				
Query 61	KKVADALTNVAHVDDMPNALSALSDLHAHKLRVDPVNFKLLSHCLLVTLAAHL				
Sbjct 61	KKVADALTNVAHVDDMPNALSALSDLHAHKLRVDPVNFKLLSHCLLVTLAAHL				
Query 121	AVHASLDKFLASVSTVLTSKYR 142				
Sbjct 121	AVHASLDKFLASVSTVLTSKYR 142				

8

Protein sequence alignment

Two biologically related proteins with similar sequences:

FlgA1 EAGNVKLKRGRDLTPPRTVLDINQLVDAISLRDLSPDQPIQLTQFRQAWRVKAGQQRVNVIASGD
++K+K+GRDLTPP +L+ N A+SLR ++ QP+ R+ W +KAGQ V V+A G+
FlgA2 TLQDIKMKQGRDLTPPGALLEPNFAQGAVSLRQINAGQPLTRNMLRRLWI KAGQDVQVLALGE

Also biologically related (& fold up into the same 3D protein structure):

FlgA1 EAGNVKLKRGRDLTPPRTVLDINQLVDAISLRDLSPDQPIQLTQFRQAWRVKAGQQRVNVIASGD
A + P +L I+ R L P + I R+AW V+ G V V
FlgA3 LAALKQVTTLIAGKHKPDAMATHAEELQGKIAKRTLLPGRYIPTAAIREAWLVEQGA AVQVFFIAG

But these are biologically unrelated (& fold up into unrelated structures):

FlgA1 AGNVKLKRGRDLTPPRTVLDINQLVDAISLRDLSPDQPIQLTQFRQA-WRVKAGQQRVNVIASGD
AG+V K G + + PRT ++ I+ P PI +++A WRV A + V V+ GD
HvcPP AGHV--KNGTMRIVGPRTCSNVWNGTFPINATTGPSIPI PAPNYKKALWRVSATEYVEVVRVGD

(FYI, we'll draw examples from Durbin *et al.*, *Biological Sequence Analysis*, Ch. 1 & 2).

9

To align two sequences, we need to perform 3 steps:

1. We need some way to decide which alignments are better than others.
For this, we'll invent a way to give the alignments a "score" indicating their quality.
2. Align the two proteins so that they get the best possible score.
3. Decide if the score is "good enough" for us to believe the alignment is biologically significant.

10

To align two sequences, we need to perform 3 steps:

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3. Decide if the score is "good enough" for us to believe the alignment is biologically significant.

11

We'll treat mutations as independent events.

This allows us to create an ***additive scoring scheme***.

The score for a sequence alignment will be the sum of the scores for aligning each of the individual positions in two sequences.

What kind of mutations should we expect?

12

Substitutions, insertions and deletions.

Insertions and deletions can be treated as equivalent events by considering one or the other sequence as the reference, and are usually called ***gaps***.

AGNVKLKRG
AG+V K G
AGHV - - KNG

substitution *gap*

13

Let's consider two models:

First, a **random** model, where amino acids in the sequences occur independently at some given frequencies.

The probability of observing an alignment between x and y is just the product of the frequencies (q) with which we find each amino acid.

We can write this as:

What does the capital pi mean?

$$P(x, y | R) = \prod_i q_{x_i} \prod_j q_{y_j}$$

What's this mean? What's this mean?

14

Second, a **match** model, where amino acids at a given position in the alignment arise from some common ancestor with a probability given by the joint probability p_{ab} .

So, under this model, the probability of the alignment is the product of the probabilities of seeing the individual amino acids aligned.

We can write that as:

What does the capital pi mean again?

$$P(x, y | M) = \prod_i p_{x_i y_i}$$

What's this mean?

What's this mean?

15

To decide which model better describes an alignment, we'll take the ratio:

$$\frac{P(x, y | M)}{P(x, y | R)} = \frac{\prod_i p_{x_i y_i}}{\prod_i q_{x_i} \prod_j q_{y_j}} = \prod_i \frac{p_{x_i y_i}}{q_{x_i} q_{y_i}}$$

What did these mean again?

Such a ratio of probabilities under 2 different models is called an **odds ratio**.

Where else have you heard odds ratios used?

Basically: if the ratio > 1 , model M is more probable
if < 1 , model R is more probable.

16

Now, to convert this to an additive score S , we can simply take the logarithm of the odds ratio (called the **log odds ratio**):

$$S = \sum_i s(x_i, y_i)$$

This is just the score for aligning one amino acid with another amino acid:

$$s(a, b) = \log \left(\frac{p_{ab}}{p_a p_b} \right)$$

Here written a and b rather than x_i and y_i to emphasize that this score reflects the inherent preference of the two amino acids (a and b) to be aligned.

Almost done with step 1...

17

The last trick:

Take a big set of pre-aligned protein sequence alignments (that are correct!) and measure all of the pairwise amino acid substitution scores (the $s(a, b)$'s). Put them in a 20x20 **amino acid substitution matrix** :

	A	R	N	D	C	Q	E	G	H	I	L	K	M	F	P	S	T	W	Y	V
A	5	-2	-1	-2	-1	-1	-1	0	-2	-1	-2	-1	-1	-3	-1	1	0	-3	-2	0
R	-2	7	-1	-2	-4	1	0	-3	0	-4	-3	3	-2	-3	-3	-1	-1	-3	-1	-3
N	-1	-1	7	2	-2	0	0	0	1	-3	-4	0	-2	-4	-2	1	0	-4	-2	-3
D	-2	-2	2	8	-4	0	2	-1	-1	-4	-4	-1	-4	-5	-1	0	-1	-5	-3	-4
C	-1	-4	-2	-4	13	-3	-3	-3	-3	-2	-2	-3	-2	-2	-4	-1	-1	-5	-3	-1
Q	-1	1	0	0	-3	7	2	-2	1	-3	-2	2	0	-4	-1	0	-1	-1	-1	-3
E	-1	0	0	2	-3	2	6	-3	0	-4	-3	1	-2	-3	-1	-1	-1	-3	-2	-3
G	0	-3	0	-1	-3	-2	-3	8	-2	-4	-4	-2	-3	-4	-2	0	-2	-3	-3	-4
H	-2	0	1	-1	-3	1	0	-2	10	-4	-3	0	-1	-1	-2	-1	-2	-3	2	-4
I	-1	-4	-3	-4	-2	-3	-4	-4	-4	5	2	-3	2	0	-3	-3	-1	-3	-1	4
L	-2	-3	-4	-4	-2	-2	-3	-4	-3	2	5	-3	3	1	-4	-3	-1	-2	-1	1
K	-1	3	0	-1	-3	2	1	-2	0	-3	-3	6	-2	-4	-1	0	-1	-3	-2	-3
M	-1	-2	-2	-4	-2	0	-2	-3	-1	2	3	-2	7	0	-3	-2	-1	-1	0	1
F	-3	-3	-4	-5	-2	-4	-3	-4	-1	0	1	-4	0	8	-4	-3	-2	1	4	-1
P	-1	-3	-2	-1	-4	-1	-1	-2	-2	-3	-4	-1	-3	-4	10	-1	-1	-4	-3	-3
S	1	-1	1	0	-1	0	-1	0	-1	-3	-3	0	-2	-3	-1	5	2	-4	-2	-2
T	0	-1	0	-1	-1	-1	-1	-2	-2	-1	-1	-1	-1	-2	-1	2	5	-3	-2	0
W	-3	-3	-4	-5	-5	-1	-3	-3	-3	-2	-3	-1	1	-4	-4	-3	15	2	-3	
Y	-2	-1	-2	-3	-3	-1	-2	-3	2	-1	-1	-2	0	4	-3	-2	-2	2	8	-1
V	0	-3	-3	-4	-1	-3	-3	-4	-4	4	1	-3	1	-1	-3	-2	0	-3	-1	5

18

This is the **BLOSUM50** matrix.

(The numbers are scaled & rounded off to the nearest integer):

What's the score for aspartate (D) aligning with itself?

How about aspartate with phenylalanine (F)? Why?

	A	R	N	D	C	Q	E	G	H	I	L	K	M	F	P	S	T	W	Y	V
A	5	-2	-1	-2	-1	-1	-1	0	-2	-1	-2	-1	-1	-3	-1	1	0	-3	-2	0
R	-2	7	-1	-2	-4	1	0	-3	0	-4	-3	3	-2	-3	-3	-1	-1	-3	-1	-3
N	-1	-1	7	2	-2	0	0	0	1	-3	-4	0	-2	-4	-2	1	0	-4	-2	-3
D	-2	-2	2	8	-4	0	2	-1	-1	-4	-4	-1	-4	-5	-1	0	-1	-5	-3	-4
C	-1	-4	-2	-4	13	-3	-3	-3	-3	-2	-2	-3	-2	-2	-4	-1	-1	-5	-3	-1
Q	-1	1	0	0	-3	7	2	-2	1	-3	-2	2	0	-4	-1	0	-1	-1	-1	-3
E	-1	0	0	2	-3	2	6	-3	0	-4	-3	1	-2	-3	-1	-1	-1	-3	-2	-3
G	0	-3	0	-1	-3	-2	-3	8	-2	-4	-4	-2	-3	-4	-2	0	-2	-3	-3	-4
H	-2	0	1	-1	-3	1	0	-2	10	-4	-3	0	-1	-1	-2	-1	-2	-3	2	-4
I	-1	-4	-3	-4	-2	-3	-4	-4	-4	5	2	-3	2	0	-3	-3	-1	-3	-1	4
L	-2	-3	-4	-4	-2	-2	-3	-4	-3	2	5	-3	3	1	-4	-3	-1	-2	-1	1
K	-1	3	0	-1	-3	2	1	-2	0	-3	-3	6	-2	-4	-1	0	-1	-3	-2	-3
M	-1	-2	-2	-4	-2	0	-2	-3	-1	2	3	-2	7	0	-3	-2	-1	-1	0	1
F	-3	-3	-4	-5	-2	-4	-3	-4	-1	0	1	-4	0	8	-4	-3	-2	1	4	-1
P	-1	-3	-2	-1	-4	-1	-1	-2	-2	-3	-4	-1	-3	-4	10	-1	-1	-4	-3	-3
S	1	-1	1	0	-1	0	-1	0	-1	-3	-3	0	-2	-3	-1	5	2	-4	-2	-2
T	0	-1	0	-1	-1	-1	-1	-2	-2	-1	-1	-1	-1	-2	-1	2	5	-3	-2	0
W	-3	-3	-4	-5	-5	-1	-3	-3	-3	-3	-2	-3	-1	1	-4	-4	-3	15	2	-3
Y	-2	-1	-2	-3	-3	-1	-2	-3	2	-1	-1	-2	0	4	-3	-2	-2	2	8	-1
V	0	-3	-3	-4	-1	-3	-3	-4	-4	4	1	-3	1	-1	-3	-2	0	-3	-1	5

19

Using this matrix, **we can score any alignment as the sum of scores of individual pairs of amino acids.**

For example, the top alignment in our earlier example:

```

FlgA1 EAGNVKLKRGRLDTLPPRTVLVDINQLVDAISLRDLSPDQPIQLTQFRQAWRVKAGQVRVNVIASGD
      ++K+K+GRLDTLPP  +L+ N    A+SLR ++  QP+      R+ W +KAGQ V V+A G+
FlgA2 TLQDIKMKQGRLDTLPPGALLEPNFAQGAVSLRQINAGQPLTRNMLRRLWIIKAGQDVQVLALGE
  
```




gets the score:

$$S(\text{FlgA1}, \text{FlgA2}) = -1 - 2 - 2 + 2 + 4 + 6 + \dots = 186$$

We also need to penalize **gaps**. For now, let's just use a constant penalty **d** for each amino acid gap in an alignment, *i. e.*:

the penalty for a gap of length $g = -g \cdot d$

20

PAM	vs.	BLOSUM
		 
Margaret Dayhoff (1925-1983) Developed point accepted mutation matrices (PAM matrices)		Steve and Jorja Henikoff Developed BLOSUM matrices
<u>Calibrated for different evolutionary times</u> PAM- n = n substitutions per 100 residues e.g. matrices from PAM1 to PAM250 measure PAM1, calculate higher PAMs from that		<u>Calibrated for different % identity sequences</u> BLOSUM- n = for sequences of about n % identity averages substitution probabilities over sequence clusters, gives better estimates for highly divergent cases
<u>Explicit model of evolution</u> (calculated using a phylogenetic tree)		<u>Implicit model of evolution</u> (calculated from blocks of aligned sequences)

21

To align two sequences, we need to perform 3 steps:

1. We need some way to decide which alignments are better than others.
For this, we'll invent a way to give the alignments a "score" indicating their quality.
2. Align the two proteins so that they get the best possible score.
3. Decide if the score is "good enough" for us to believe the alignment is biologically significant.

22

A sense of scale:

There are $\binom{2n}{n} \approx \frac{2^{2n}}{\sqrt{\pi n}}$ possible global alignments between two sequences of length n if we use gaps

So, with 2 sequences of length 100, that's $> 10^{60}$ possible alignments

23

We'll use something called ***dynamic programming***.

This is **mathematically guaranteed** to find the best scoring alignment, and uses ***recursion***. This means problems are broken into sub-problems, which are in turn broken into sub-problems, etc, until the simplest sub-problems can be solved.

We're going to find the best ***local*** alignment—the best matching internal alignment—without forcing all of the amino acids to align (i.e. to match ***globally***).

i.e., this \longrightarrow ATGCAT
 ATGCAT

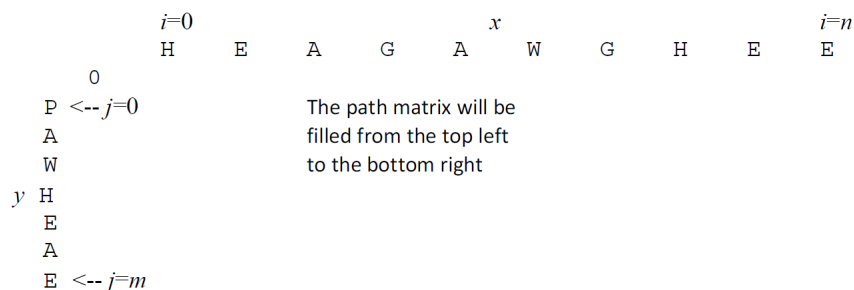
Not this \longrightarrow ACGTTATGCATGACGTA
 -C---ATGCAT----T-

24

Here's the main idea:

We'll make a **path matrix**, showing the possible alignments and their scores. There are simple rules for how to fill in the matrix.

This will test all possible alignments & give us the top-scoring alignment between the two sequences.



25

Here are the rules:

For a given square in the matrix $F(i,j)$, we look at the squares to its left $F(i-1,j)$, top $F(i,j-1)$, and top-left $F(i-1,j-1)$. Each should have a score.

We consider **3 possible events** & **choose the one scoring the highest**:

(1) x_i is aligned to y_j

$$F(i-1,j-1) + s(x_i, y_j)$$

(2) x_i is aligned to a gap

$$F(i-1,j) - d$$

(3) y_j is aligned to a gap

$$F(i,j-1) - d$$

For this example, we'll use $d = 8$. We also set the left-most & top-most entries to zero.

26

Just two more rules:

If the score is negative, set it equal to zero.

At each step, we also keep track of which event was chosen by **drawing an arrow from the cell we just filled back to the cell which contributed its score to this one.**

That's it! Just repeat this to fill the entire matrix.

27

Here we go! Start with the borders & the first entry.

		H	E	A	G	A	W	G	H	E	E
	0	0	0	0	0	0	0	0	0	0	0
P	0	0									
A	0										
W	0										
H	0										
E	0										
A	0										
E	0										

Why is this zero?

What's the score from our BLOSSUM matrix for substituting H for P?

28

Next round!

		H	E	A	G	A	W	G	H	E	E
	0	0	0	0	0	0	0	0	0	0	0
P	0	0	0								
A	0	0	0								
W	0										
H	0										
E	0										
A	0										
E	0										

Terrible! Again, none of the possible give positive scores.
We have to go a bit further in before we find a positive score...

29

A few more rounds, and a positive score at last!

		H	E	A	G	A	W	G	H	E	E
	0	0	0	0	0	0	0	0	0	0	0
P	0	0	0	0							
A	0	0	0	5							
W	0	0	0								
H	0										
E	0										
A	0										
E	0										

How did we get this one?

30

& a few more rounds...

		H	E	A	G	A	W	G	H	E	E
	0	0	0	0	0	0	0	0	0	0	0
P	0	0	0	0	0						
A	0	0	0	5	0						
W	0	0	0	0	2						
H	0	10	2	0	0						
E	0										
A	0										
E	0										

What does this mean?

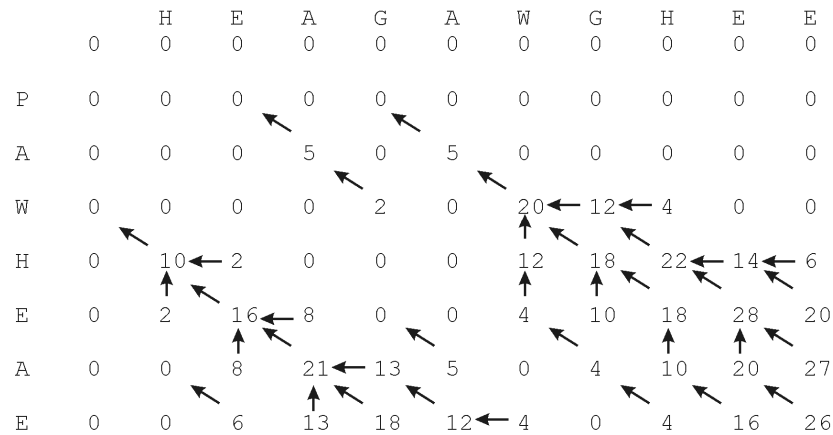
31

The whole thing filled in!

		H	E	A	G	A	W	G	H	E	E
	0	0	0	0	0	0	0	0	0	0	0
P	0	0	0	0	0	0	0	0	0	0	0
A	0	0	0	5	0	5	0	0	0	0	0
W	0	0	0	0	2	0	20	12	4	0	0
H	0	10	2	0	0	0	12	18	22	14	6
E	0	2	16	8	0	0	4	10	18	28	20
A	0	0	8	21	13	5	0	4	10	20	27
E	0	0	6	13	18	12	4	0	4	16	26

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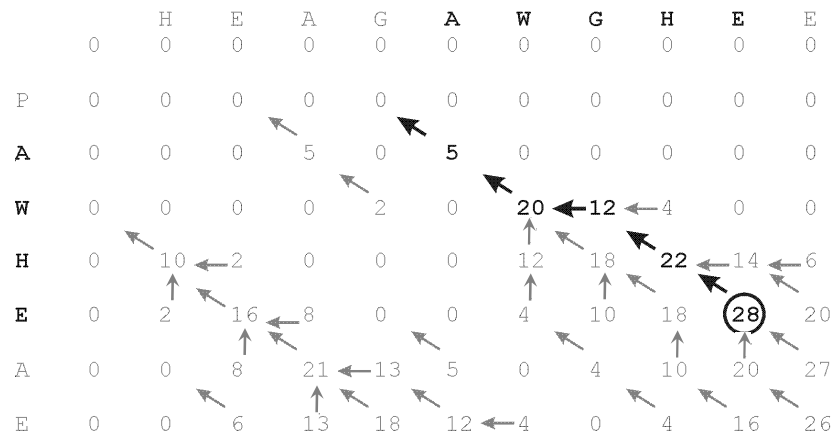
Now, find the optimal alignment using a **traceback** process:
Look for the highest score, then follow the arrows back.
The alignment “grows” from right to left



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This gives the following alignment: **AWGHE**
 AW-HE

(Note: for gaps, the arrow points to the sequence that gets the gap)



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To align two sequences, we need to perform 3 steps:

1. We need some way to decide which alignments are better than others.
For this, we'll invent a way to give the alignments a "score" indicating their quality.
2. Align the two proteins so that they get the best possible score.
3. **Decide if the score is "good enough" for us to believe the alignment is biologically significant.**

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This algorithm always gives the best alignment.

Every pair of sequences can be aligned in some fashion.

So, when is a score "good enough"?

How can we figure this out?

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Here's one approach:

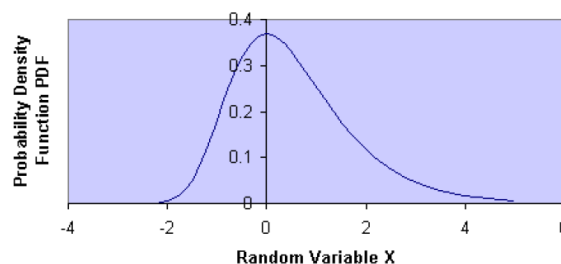
**Shuffle one sequence. Calculate the best alignment & its score.
Repeat 1000 times.**

If we never see a score as high as the real one, we say the real score has <1 in a 1000 chance of happening just by luck.

But if we want something that only occurs < 1 in a million, we'd have to shuffle 1,000,000 times...

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Luckily, alignment scores follow a well-behaved distribution, the **extreme value distribution**, so we can do a few trials & fit to this.



random trials & their average score

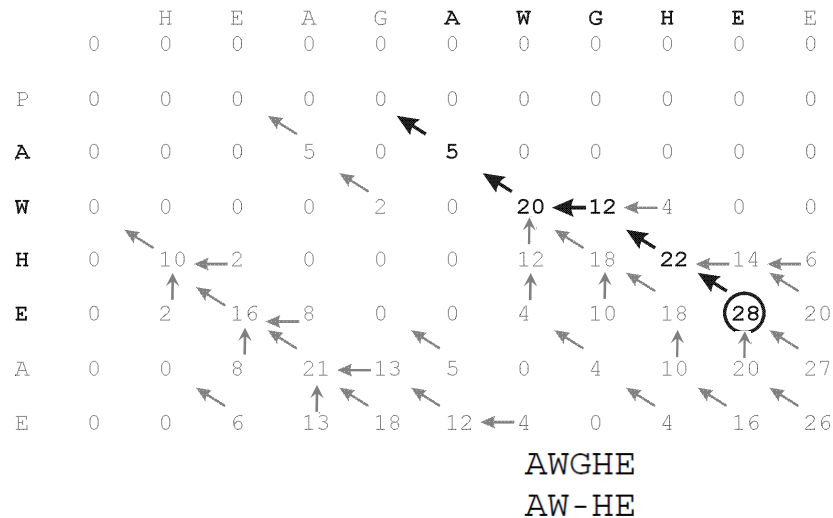
$$p(\text{max score} \leq X) \approx e^{-kNe^{\lambda(X-\mu)}}$$

This p-value gives the significance of your alignment.
But, if we search a database and perform many alignments, we still need something more (next time).

Describe the shape & can be fit from a few trials

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Some extensions: Local vs. global alignments
How might you force the full sequences to align?



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Some extensions: Local vs. global alignments
How might you force the full sequences to align?

A few tiny changes:

Initialize only the top left cell of the path matrix to zero
(not all top and left cells).

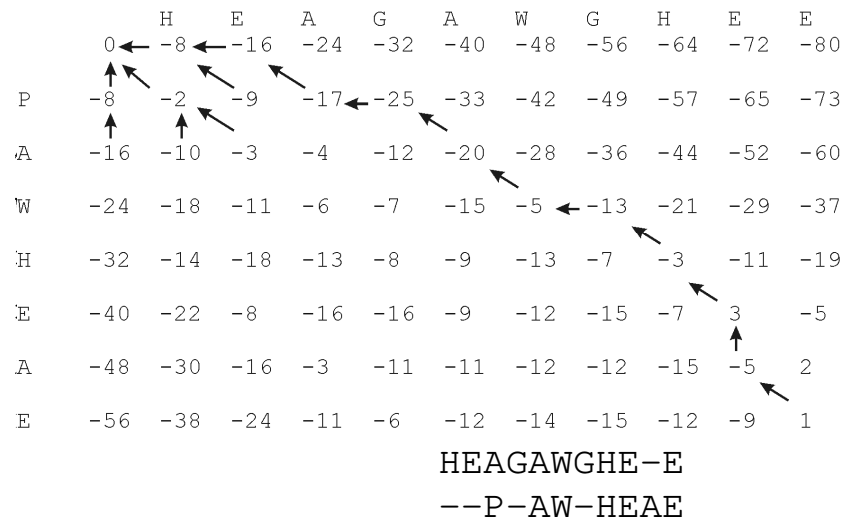
Leave the negative values (don't set them to zero).

The optimal alignment should start at the top left cell and
finish at the bottom right cell of the path matrix.

Start the trace-back at the bottom right cell

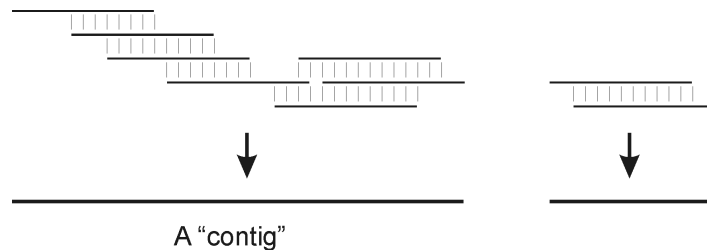
40

Some extensions: Local vs. global alignments
How might you force the full sequences to align?



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Some extensions:
What about overlapping sequences?
e.g. as in 'shotgun sequencing' genomes where
'contigs' are built up from overlapping sequences



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Some extensions:

What about overlapping sequences?

Modify global alignment to not penalize overhangs:

The optimal alignment should start at the top or left edge and finish at the bottom or right edge of the path matrix.

Set these boundary conditions :

$$F(i,0) = 0 \text{ for } i=1 \text{ to } n$$

$$F(0,j) = 0 \text{ for } j=1 \text{ to } m$$

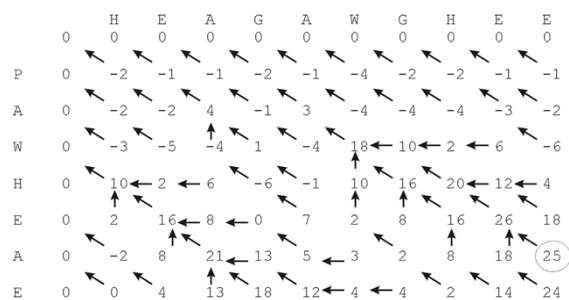
Start the traceback at the cell with the highest score on the right or bottom border

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Some extensions:

What about overlapping sequences?

e.g. as in 'shotgun sequencing' genomes where 'contigs' are built up from overlapping sequences



(overhang = HEA)

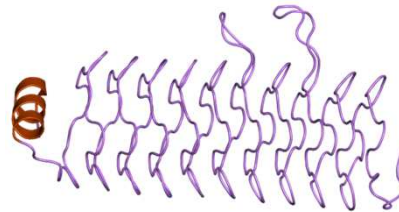
GAWGHEE

PAW-HEA

(overhang = E)

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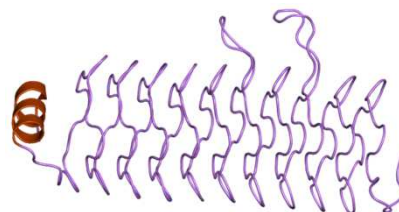
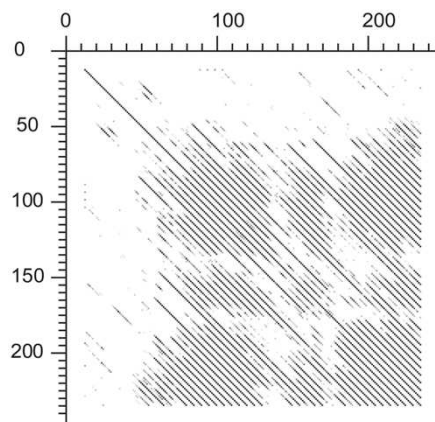
Some extensions:
How might you find repetitive sequences?



Structure of the pentapeptide
repeat protein HetL
(from wiki, PMID18952182)

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Align the sequence to itself and ignore the diagonal (optimal) alignment
→ High-scoring off-diagonal alignments will be repeats



Structure of the pentapeptide
repeat protein HetL
(from wiki, PMID18952182)

Dot plot (quick visualization of
sequence similarity)
of the pentapeptide repeat
protein HgIK protein vs. itself
(http://en.wikipedia.org/wiki/Pentapeptide_repeat)

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